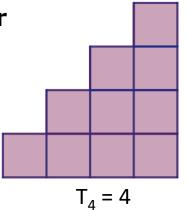






# Triangular numbers can be represented by a triangular array of squares.

Imagine two copies of a triangular array of squares. Can you picture how to fit them together to make a rectangle? What is special about the dimensions of your rectangle?



- Start by drawing a triangle number. Can you draw the same triangle number so the two fit together to make a rectangle?

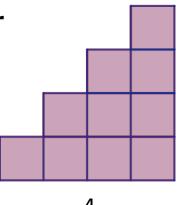
  Unsure? Click
- 2 Write down the dimensions of your rectangle.
- 3 Try this a few more times with different triangles. Keep labelling the dimensions.
- 4 What do you notice about the dimensions of the rectangles?
- 5 Find the area of one of your rectangles.
- 6 What is the connection between the area of the triangle and the rectangle?

#### <u>Answers</u>



Triangular numbers can be represented by a triangular array of squares.

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4

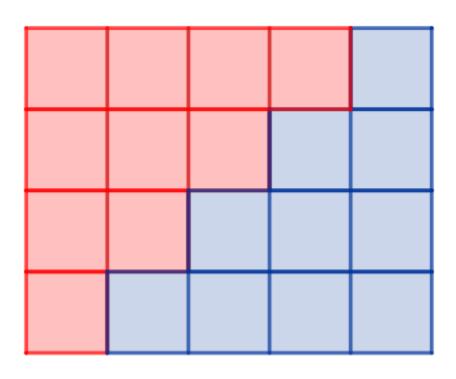
4 What do you notice about the dimensions of the rectangles?

The length is 1 more that the width.

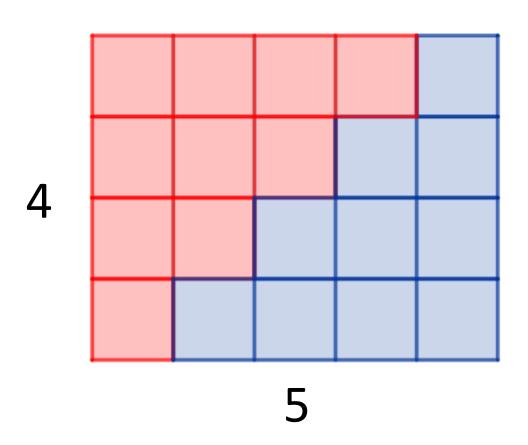
- Find the area of one of your rectangles. E.g.  $4 \times 5 = 20 \text{ cm}^2$
- 6 What is the connection between the area of the triangle and the rectangle?

The area of the triangle is half the area of the rectangle.









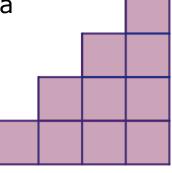
The length is one more than the width.

This should be the case for all your other examples too.



The pattern on the right is the fourth triangle number. It has a base of 4 units. It can be expressed as  $T_4$ 

Lets use algebra to explain this.



- Lets say the base of a triangle array of squares is **n** units across.
  - What are the dimensions of the rectangle now?

$$T_n = n$$

- 2 What would be the area of the rectangle?
- What would the area of the triangle be?

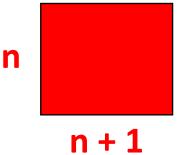
#### **Answers**



The pattern on the right is the fourth triangle number. It has a base of 4 units. It can be expressed as  $T_4$ 

#### Lets use algebra to explain this.

- Lets say the base of a triangle array of squares is n units across. What are the dimensions of the rectangle now?  $T_n = n$
- 2 What would be the area of the rectangle?



What would the area of the triangle be?

$$\frac{n\times(n+1)}{2}$$

— The triangle is half the area of the rectangle



#### Lets test this formula!

$$T_n = \frac{n \times (n+1)}{2}$$

Find the  $10^{th}$  triangle number by substituting n = 10 into the formula.

2 Can this number be arranged into a triangle?

#### Lets test this formula!

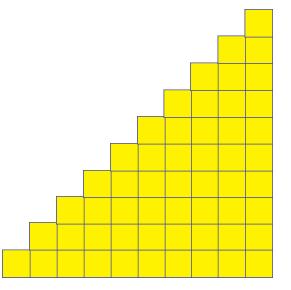
$$T_n = \frac{n \times (n+1)}{2}$$

Find the  $10^{th}$  triangle number by substituting n = 10 into the formula.

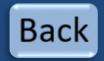
$$T_{10} = \frac{10 \times (10 + 1)}{2} = 55$$

2 Can this number be arranged into a triangle?

$$T_{10} = 55$$



#### End of the lesson



#### Well done for completing the lesson.

